Learning-Based Multiuser Scheduling in MIMO-OFDM Systems with Hybrid Beamforming

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Abstract—We investigate the multiuser scheduling problem in multiple-input multiple-output (MIMO) systems using orthogonal frequency division multiplexing (OFDM) and hybrid beamforming in which a base station (BS) communicates with multiple users over millimeter wave (mmWave) channels in the downlink. Improved scheduling is critical for enhancing spectral efficiency and the long-term performance of the system from the perspective of proportional fairness (PF) metric in hybrid beamforming systems due to its limited multiplexing gain. Our objective is to maximize PF by properly designing the analog and digital precoders within the hybrid beamforming and selecting the users subject to the number of radio frequency (RF) chains. Leveraging the characteristics of mmWave channels, we apply a two-timescale protocol. On a long timescale, we assign an analog beam to each user. Scheduling the users and designing the digital precoder are done accordingly on a short timescale. To conduct scheduling, we propose combinatorial solutions, such as greedy and sorting algorithms, followed by a machine learning (ML) approach. Our numerical results highlight the trade-off between the performance and complexity of the proposed approaches. Consequently, we show that the choice of approach depends on the specific criteria within a given scenario.

I. INTRODUCTION

Millimeter wave (mmWave) frequency band is a promising candidate for 5G and beyond [1]. However, mmWave signals are inherently susceptible to high path loss, necessitating base stations (BSs) to be equipped with large antenna arrays and beamforming techniques to mitigate interference and enhance spectral efficiency. Hybrid beamforming has gained traction as a viable solution in mmWave systems, offering fewer required radio frequency (RF) chains. Hybrid beamforming enables improved management of multiuser interference and strikes a better balance of performance and efficiency than conventional analog and digital beamforming [2]. Nevertheless, the reduced number of RF chains restricts the multiplexing gain in multiuser systems and limits the maximum number of users that each BS can simultaneously serve. Consequently, multiuser scheduling becomes essential such that the BS could dynamically select a subset of users to serve at each time.

The literature contains several studies on hybrid beamforming and user scheduling as part of radio resource management (RRM) for multiple-input multiple-output (MIMO) systems. The hybrid beamforming problem has been explored in [2]– [5]. In [2], the authors assume that the number of users is no greater than that of RF chains. Moreover, in [3]–[5], it is assumed that the BS serves a single user, where scheduling is unnecessary. On the other hand, studies such as [6]–[9] have investigated the hybrid beamforming and user scheduling as a joint problem under the assumption that the number of users exceeds the available RF chains. That being said, a flatfading channel model is adopted in [6]–[8] for mmWave hybrid beamforming systems. In practice, this channel model is less realistic for real-world applications. Addressing this issue, the authors in [9] have considered a frequency-selective model and formulated the joint user scheduling and hybrid beamforming based on orthogonal frequency division multiplexing (OFDM) systems. As two major limitations, their approach only relies on an offline solution for a relaxed problem, which may be impractical. It also lacks a comprehensive comparison of the performance and complexity across different methods.

This paper falls within the realms of joint hybrid beamforming and user scheduling in MIMO-OFDM systems. We build on the work presented in [8] and extend it to OFDM systems under frequency-selective fading models. We utilize a two-timescale protocol to solve the joint problem of hybrid beamforming and user scheduling. To select a subset of users, we leverage various combinatorial methods along with a machine learning (ML) approach, each offering distinct performance and complexity profiles. Our numerical results reveal that, in terms of longterm proportional fairness and required run time, one of these approaches may be more suitable depending on its delivered trade-off between performance and complexity.

II. SYSTEM MODEL

We consider a downlink multiuser system in which a BS communicates with I users in a time-slotted manner over MIMO mmWave channels (Fig. 1). We assume the channels follow a *frequency-selective* fading model. Therefore, we exert OFDM technology and adopt a hybrid beamforming architecture at the BS assisted by $N_{\rm TX}$ antennas and $N_{\rm RF}$ RF chains, where $N_{\rm RF} < N_{\rm TX}$. In this model, every user has $N_{\rm RX}$ antennas and a single RF chain. Each RF chain at the BS is linked to an independent OFDM resource grid that consists of K physical resource blocks (PRBs) within a single slot. Every PRB has several subcarriers with equal bandwidths. We assume that one¹ user is scheduled per resource grid at each slot and define $I_{\rm max} \leq I$. Thus, we have $I_{\rm max} = N_{\rm RF}$,

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¹This assumption distinguishes between OFDM and orthogonal frequency division multiple access (OFDMA). OFDMA allows scheduling multiple users within each resource grid. However, we keep this technology for future studies.



Fig. 1: A multiuser MIMO-OFDM system in downlink.

and the spatial multiplexing gain of the considered hybrid beamforming system is limited by $\min\{N_{\rm RF}, I\} = N_{\rm RF}$ [2]. At the time slot $t, \forall t \in \mathbb{N}$, a *user scheduler* at the BS selects a subset of users to be served, which is denoted by $\mathcal{M}(t)$ with the size of $|\mathcal{M}(t)| = M(t)$ such that $M(t) \leq I_{\rm max}$, and

$$\mathcal{M}(t) = \{ i_m \mid \forall m = 1, 2, ..., M(t) \}.$$
 (1)

At the BS, a module with $N_{\rm RF}$ antenna port mappers first maps M(t) selected users' data streams to the inputs of Kdigital (baseband) precoders. In this context, an antenna port can be seen as a logical entity associated with an independent resource grid. Thus, each antenna port is uniquely assigned to one of the selected users and maps the modulated symbols of that user's data stream to K PRBs, with each symbol being mapped to one distinct subcarrier within a PRB. Subsequently, the k-th precoder, where $k = 1, 2, \ldots, K$, applies baseband precoding to all selected users' symbols arranged side-by-side in the k-th PRB. In this regard, the precoding matrix of the k-th baseband precoder at the t-th slot is denoted by $\mathbf{F}_k(t)$ and defined as follows

$$\mathbf{F}_{k}(t) = [\mathbf{f}_{k,i_{1}}(t), ..., \mathbf{f}_{k,i_{M(t)}}(t)] \in \mathbb{C}^{M(t) \times M(t)}.$$
 (2)

Afterward, inverse fast Fourier transform (IFFT) and cyclic prefix (CP) adder modules followed by an RF chain at each terminal port dedicated to one selected user construct an OFDM symbol from K digitally precoded symbols of that user. We consider a fully connected structure in which all RF chains are connected to all antennas. Therefore, M(t) OFDM signals are jointly precoded via an *analog precoder* under the precoding matrix $\mathbf{G}(t)$ defined as

$$\mathbf{G}(t) = [\mathbf{g}_{i_1}(t), \dots, \mathbf{g}_{i_{M(t)}}(t)] \in \mathbb{C}^{N_{\mathrm{TX}} \times M(t)}.$$
 (3)

The analog precoder typically adopts a beamforming *codebook* $\mathcal{G} = \{\psi_{\ell} \mid \ell = 1, 2, \dots, |\mathcal{G}|\}$ in mmWave.² In this scenario, $\psi_{\ell} \in \mathbb{C}^{N_{\mathrm{TX}} \times 1}$ represents the ℓ -th analog beamforming vector. Following the user scheduling, the corresponding beamforming vector for the user $i_m \in \mathcal{M}(t)$ is selected from the codebook, i.e., $\mathbf{g}_{i_m}(t) \in \mathcal{G}$ at the *t*-th slot.

Once the analog beamforming is performed, an outcome signal $\mathbf{x}_k(t) \in \mathbb{C}^{N_{\text{TX}} \times 1}$ is transmitted via an antenna array within the k-th PRB at the t-th slot, which is modeled as

$$\mathbf{x}_{k}(t) = \mathbf{G}(t)\mathbf{F}_{k}(t)\mathbf{s}_{k}(t)$$
$$= \mathbf{G}(t)\sum_{i_{m}\in\mathcal{M}(t)}\mathbf{f}_{k,i_{m}}(t)s_{k,i_{m}}(t)$$
(4)

²The codebook is defined since phase shifters take quantized angles [2].

where $\mathbf{s}_k(t) = [s_{k,i_1}(t), ..., s_{k,i_M(t)}(t)] \in \mathbb{C}^{M(t) \times 1}$ with $s_{k,i_m}(t) \in \mathbb{C}$ being the data stream of the user $i_m \in \mathcal{M}(t)$ to be transmitted within the k-th PRB. Here, $\mathbb{E}[|s_{k,i_m}(t)|^2] = 1$, and $\mathbb{E}[s_{k,i_m}^*(t)s_{k,j_m}(t)] = 0$ for $i_m \neq j_m \in \mathcal{M}(t)$. With regard to (4), the transmission power of the BS is truncated as $\mathbb{E}[|\mathbf{x}_k(t)|^2] \leq P_k$ with $P_k \in \mathbb{R}^+$ indicating the power limit at the k-th PRB. Let us define $\mathbf{h}_{k,i_m}(t) \in \mathbb{C}^{N_{\text{TX}} \times N_{\text{RX}}}$ as the channel matrix between the BS and the i_m -th user through the k-th PRB at the t-th slot. The final processed signal $y_{k,i_m}(t) \in \mathbb{C}$ at that user is derived as

$$y_{k,i_m}(t) = \widehat{\mathbf{g}}_{i_m}^H(t) \mathbf{h}_{k,i_m}^H(t) \mathbf{x}_k(t) + \widehat{\mathbf{g}}_{i_m}^H(t) \mathbf{n}_{i_m}(t)$$
(5)

where $\mathbf{n}_{i_m}(t) \sim \mathcal{CN}(0, \sigma_{i_m}^2) \in \mathbb{C}^{N_{\mathrm{RX}} \times 1}$ is a white Gaussian noise, and $\sigma_{i_m}^2$ shows the noise power. In addition, $\widehat{\mathbf{g}}_{i_m}(t) \in \mathbb{C}^{N_{\mathrm{RX}} \times 1}$ denotes the analog combining vector that an *analog combiner* at the user derives and then applies to the received signal. Importing (5) into (4), the achievable rate for the user $i_m \in \mathcal{M}(t)$ is computed as

$$r_{i_m}(t) = \sum_{k=1}^{K} B_k \log_2(1 + \text{SINR}_{k,i_m}) \quad [\text{bits/sec/Hz}] \quad (6)$$

at the *t*-th slot, whereas $r_{j_m}(t) = 0$, $\forall j_m \notin \mathcal{M}(t)$. In (6), B_k denotes the *bandwidth factor* of the *k*-th PRB, where its value is equal to the product of the number of subcarriers per PRB and the number of OFDM symbols per slot. Also, we have

$$\operatorname{SINR}_{k,i_m} = \frac{|\mathbf{u}_{k,i_m}(t)\mathbf{f}_{k,i_m}(t)|^2}{\sum_{j_m \in \mathcal{M}(t) \setminus \{i_m\}} |\mathbf{u}_{k,i_m}(t)\mathbf{f}_{k,j_m}(t)|^2 + \sigma_{i_m}^2}$$
(7)

where $\mathbf{u}_{k,i_m}(t) = [u_{k,i_mj_1}, ..., u_{k,i_mj_m}]^H \in \mathbb{C}^{M(t) \times 1}$ with its element $u_{k,i_mj_m} = \widehat{\mathbf{g}}_{i_m}^H(t) \mathbf{h}_{k,i_m}^H(t) \mathbf{g}_{j_m}(t) \in \mathbb{C}, \forall i_m, j_m \in \mathcal{M}(t)$, which is called an *effective channel*.

III. PROPORTIONAL FAIRNESS MAXIMIZATION

Within this section, we first define a *proportional fairness* (PF) metric and then formulate the optimization problem.

A. The PF Metric

Let us consider $R_i(T) = (1 - \eta_i)R_i(T - 1) + \eta_i r_i(T)$ the cumulative data rate of the *i*-th user within the period of *T* time slots in the form of an exponential moving average of the rates [10], where $r_i(t)$ denotes the instantaneous rate from (6), and $0 \le \eta_i \le 1$ is a tuning factor. To initialize, we have $R_i(0) = 1$ for i = 1, 2, ..., I. The PF metric is defined as

$$PF = \sum_{i=1}^{I} \log(R_i(T)), \qquad (8)$$

which guarantees that no user is starved completely.

B. The Optimization Problem

The long-term objective is to maximize the defined PF in (8), subject to the constraints imposed by the hybrid beamforming system. Inspired from [11], maximizing PF within the period of T slots could be decomposed into maximizing the weighted sum of instantaneous data rates, i.e., $\sum_{i=1}^{I} w_i(t)r_i(t)$ at each



Fig. 2: Structure of the two-timescale protocol for one resource grid.

slot t = 1, 2, ..., T, as consecutive *one-shot* problems. In this context, we consider $w_i(t) = 1/R_i(t-1)$, which offers user fairness such that the user scheduler would select the users that have not been served for a long time. Therefore, the one-shot problem \mathcal{P} at the *t*-th slot is formulated as follows

$$\mathcal{P}: \max_{\mathcal{M}(t), \{\mathbf{F}_{k}(t)\}_{k=1}^{K}, \mathbf{G}(t)} \sum_{i=1}^{I} w_{i}(t)r_{i}(t)$$

s.t. $\mathcal{C}_{1}: \mathcal{M}(t) \subset \{1, 2, ..., I\}, \quad \mathcal{C}_{2}: |\mathcal{M}(t)| \leq I_{\max},$
 $\mathcal{C}_{3}: \sum_{i_{m} \in \mathcal{M}(t)} \|\mathbf{G}(t)\mathbf{f}_{k,i_{m}}(t)\|^{2} \leq P_{k}, k = 1, ..., K$
 $\mathcal{C}_{4}: \mathbf{g}_{i_{m}}(t) \in \mathcal{G}, \forall i_{m} \in \mathcal{M}(t),$ (9)

where C_1 and C_2 are user scheduling requirements, the transmission power constraint at the BS is shown in C_3 , and C_4 implies the codebook utilization for analog RF beamforming.

The problem \mathcal{P} is a mixed-integer problem (MIP) as $\mathcal{M}(t)$ and $\mathbf{G}(t)$ exist in discrete spaces, whereas $\mathbf{F}_k(t)$, for k = 1, 2, ..., K, has a continuous outcome space. The total number of possible combinations for the discrete solution variables is derived as $\sum_{i=1}^{I_{\max}} \left({I \choose i} \times |\mathcal{G}|^i \right)$, which grows fast with the increase of I_{\max} , I, and $|\mathcal{G}|$. Also, to compute the users' data rates, i.e., $r_i(t)$ from (6), the BS needs to know the channel information of all users within every PRB in advance. This requires the users to estimate their channels and share them with the BS, resulting in a large time overhead and waste of energy. To address this, we develop a *two-timescale* protocol.

IV. TAILORED TWO-TIMESCALE PROTOCOL

A. Two-Timescale Protocol

The two-timescale protocol exploits mmWave characteristics, where path gains vary slower than path angles [12]–[14]. We assume fixed path angles over long-time blocks, while correlated gains may change among shorter blocks. Given the limited number of clusters with distinct path angles in every mmWave channel, relative to N_{TX} , we can apply *directional* analog beamforming on a *long* timescale such that the highest gain of the beamformer is aligned with the dominant path angle [12]. Digital beamforming adapts to path gains on a *short* timescale, along with user scheduling at each short-time block. The two-timescale protocol is shown in Fig. 2, where a long-time block consists of N_{SB} short-time blocks for a resource grid, indexed by $t \in \mathbb{N}$. The detailed steps follow.

Step I. Analog beamforming: During the first short-time block of each long-time block, i.e., $t = 1, N_{SB} + 1, ...,$ the

BS broadcasts a pilot symbol to all users by applying each beamforming vector ψ_{ℓ} in the codebook \mathcal{G} sequentially for $\ell = 1, 2, \ldots, |\mathcal{G}|$. Then, each user selects its best beam based on the received pilots and its derived analog combining vector. The index of the best beam for the *i*-th user is derived as

$$\ell_i^*(t) = \arg \max_{\ell=1,2,\dots,|\mathcal{G}|} \frac{1}{K} \sum_{k=1}^{K} \left| \widehat{\mathbf{g}}_i^H(t) \mathbf{h}_{k,i}^H(t) \psi_\ell \right|^2.$$
(10)

Afterward, each user shares the index of its best beam with the BS, and the BS assigns an analog beamforming vector from the codebook \mathcal{G} to each user accordingly so that the analog precoder of the *i*-th user is derived as $\mathbf{g}_i^*(t) = \psi_{\ell_i^*(t)}$. From (3), $\mathbf{G}^*(t)$ is constructed at time slots $t = 1, N_{\rm SB} + 1, ...$ and fixedly used through the following $N_{\rm SB} - 1$ short-time blocks.

Step II. Acquisition of effective channels: At the *t*-th short-time block, the BS generates an effective channel matrix denoted by $\mathbf{U}_k(I;t) = [\mathbf{u}_{k,1}^*(t),...,\mathbf{u}_{k,I}^*(t)] \in \mathbb{C}^{I \times I}$. For this, the *i*-th user measures the effective channels $u_{k,ij}^* = \widehat{\mathbf{g}}_i^H(t)\mathbf{h}_{k,i}^H(t)\mathbf{g}_j^*(t) \in \mathbb{C}$ for i, j = 1, ..., I within the *k*-th PRB based on the assigned beams and then shares $\mathbf{u}_{k,i}^*(t) = [u_{k,i1}^*, ..., u_{k,iI}^*]^H \in \mathbb{C}^{I \times 1}$ for k = 1, ..., K with the BS.

Step III. User scheduling and digital beamforming: According to the assigned analog beamforming vectors, i.e., $\mathbf{G}^*(t)$, the generated effective channel matrix, i.e., $\mathbf{U}_k(I;t)$, and weights of the users, i.e., $\{w_i(t)\}_{i=1}^I$, from their cumulative data rates, the BS conducts user scheduling and digital beamforming at the *t*-th short-time block. Hence, \mathcal{P} can be reformed to reduce complexity, as discussed in Section IV-B.

Step IV. Data transmission: With the designed system, the selected user i_m , $\forall i_m \in \mathcal{M}(t)$, at the *t*-th short-time block is served under the rate of $r_{i_m}(t)$ as in (6). The weights of all users are updated based on their cumulative data rates.

Steps II to IV are repeated for $N_{\rm SB} - 1$ short-time blocks starting from the second block until the end of each long-time block, i.e., $t = 2, ..., N_{\rm SB}$ for the first long-time block.

B. Problem of User Scheduling and Digital Beamforming

We reach a new problem with reduced complexity owing to the two-timescale protocol from Section IV-A. After selecting users, i.e., $\mathcal{M}(t)$, the precoding matrix is derived as

$$\mathbf{G}^{*}(t) = [\mathbf{g}_{i_{1}}^{*}(t), ..., \mathbf{g}_{i_{M}(t)}^{*}(t)].$$
(11)

Having $\mathbf{G}^*(t)$, \mathcal{P} in (9) is transformed into a joint problem of user scheduling and digital beamforming as follows

$$\widehat{\mathcal{P}}: \max_{\mathcal{M}(t), \{\mathbf{F}_{k}(t)\}_{k=1}^{K}} \sum_{i=1}^{I} w_{i}(t)r_{i}(t) \\
\text{s.t. } \mathcal{C}_{1}: \mathcal{M}(t) \subset \{1, 2, ..., I\}, \quad \mathcal{C}_{2}: |\mathcal{M}(t)| \leq I_{\max}, \\
\mathcal{C}_{3}: \sum_{i_{m} \in \mathcal{M}(t)} \|\mathbf{G}^{*}(t)\mathbf{f}_{k,i_{m}}(t)\|^{2} \leq P_{k}, \ k = 1, ..., K. \quad (12)$$

With a given $\mathcal{M}(t)$ at the *t*-th time slot, the precoding matrix of the *k*-th digital precoder, i.e., $\mathbf{F}_k(t)$, is derived by solving $\widehat{\mathcal{P}}$ in (12), with regard to (6) and (7).

To design the digital precoder, we apply *zero-forcing* (ZF) beamforming [15], which offers near-optimal performance in

Algorithm 1: Greedy incremental user scheduling

mmWave due to the small number of clusters [2], [12]. Based on $\mathcal{M}(t)$ in hand at the *t*-th short block, the effective channel matrix is derived concerning the selected users, as below

$$\mathbf{U}_{k}(\mathcal{M}(t);t) = [\mathbf{u}_{k,i_{1}}^{*}(t), ..., \mathbf{u}_{k,i_{m}}^{*}(t)] \in \mathbb{C}^{M(t) \times M(t)}.$$
 (13)

From (13), the ZF-based digital precoder for the k-th PRB satisfies $\mathbf{U}_k(\mathcal{M}(t); t)\mathbf{F}_k(t) = \mathbf{I}_{\mathcal{M}(t)}$, where $\mathbf{I}_{\mathcal{M}(t)}$ denotes the identity matrix of size $\mathcal{M}(t)$. Thus, we can write

$$\mathbf{F}_{k}(t) = \mathbf{U}_{k}^{H}(\mathcal{M}(t);t) \Big[\mathbf{U}_{k}(\mathcal{M}(t);t) \mathbf{U}_{k}^{H}(\mathcal{M}(t);t) \Big]^{-1}.$$
 (14)

Considering a fair power allocation scheme for all M(t) data streams within each PRB, we have $\|\mathbf{G}^*(t)\mathbf{f}_{k,i_m}(t)\|^2 = \frac{P_k}{M(t)}$ for k = 1, ..., K. Hence, the beamforming vector for the user $i_m, \forall i_m \in \mathcal{M}(t)$, in $\mathbf{F}_k(t)$ is normalized such that

$$\mathbf{f}_{k,i_m}(t) = \sqrt{\frac{P_k}{M(t)} \frac{\mathbf{f}_{k,i_m}(t)}{\|\mathbf{G}^*(t)\mathbf{f}_{k,i_m}(t)\|_2}}.$$
 (15)

By the use of (11), (13)–(15), and the given $\mathcal{M}(t)$, we compute $r_{i_m}(t)$ for the user i_m , $\forall i_m \in \mathcal{M}(t)$, from (6) and (7). Accordingly, we can define $\bar{r}(\mathcal{M}(t);t) = \sum_{i_m \in \mathcal{M}(t)} w_{i_m}(t)r_{i_m}(t)$ as the weighted sum-rate of the scheduled users at the t-th block.

To conduct scheduling, we aim to find the best set of users at each short block to maximize the sum-rate at the respective slot. In this sense, a naive approach is to employ the *bruteforce* algorithm or perform an *exhaustive search* by calculating the ZF-based digital precoder for every possible combination of M(t) users and then selecting the best case that yields the highest $\bar{r}(\mathcal{M}(t);t)$. However, either algorithm demands heavy computation when dealing with large I and M(t).

V. MULTIUSER SCHEDULING DESIGN USING COMBINATORIAL APPROACHES

A. Greedy Algorithm

1) Incremental approach: The idea behind the incremental algorithm, as illustrated in Algorithm 1, is to start from an empty set $\mathcal{M}(t) = \emptyset$ at the *t*-th short-time block and add users iteratively until the performance can no longer be improved.

Within the *n*-th iteration, where $n = 1, 2, ..., I_{\text{max}}$, the *i**-th user that offers the highest weighted sum-rate is found by

$$i^* = \arg\max_{i \in \{i|i=1,2,\dots,I\} \setminus \mathcal{M}(t)} \bar{r}(\mathcal{M}(t) \cup \{i\}; t).$$
(16)

The user i^* is added to $\mathcal{M}(t)$ if it improves the performance, i.e., $\bar{r}(\mathcal{M}(t) \cup \{i^*\}; t) > \bar{r}(\mathcal{M}(t); t)$. The process terminates if $\bar{r}(\mathcal{M}(t) \cup \{i^*\}; t) \leq \bar{r}(\mathcal{M}(t); t)$ or M(t) reaches I_{\max} .

2) Decremental approach: The greedy decremental algorithm starts by initiating a full set of all users, i.e., $\mathcal{M}(t) = \{i \mid i = 1, 2, ..., I\}$, from a contrary perspective compared to the incremental algorithm. In the *n*-th arbitrary iteration, the *j*-th user that satisfies

$$j = \underset{j \in \mathcal{M}(t)}{\arg \max} \ \bar{r}(\mathcal{M}(t) \setminus \{j\}; t)$$
(17)

is removed from $\mathcal{M}(t)$. The procedure continues down to the subset of users that ensures the highest weighted sum-rate, i.e., $\bar{r}(\mathcal{M}(t) \setminus \{j\}; t) \leq \bar{r}(\mathcal{M}(t); t), \forall j \in \mathcal{M}(t)$, and $M(t) \leq I_{\text{max}}$.

The greedy incremental and decremental algorithms require M(t)(2I - M(t) + 1)/2 and (I - M(t))(I + M(t) + 1)/2 number of user searches to schedule M(t) users, respectively [16]. Thus, an increase in the number of users monotonically increases the search complexity. Additionally, recalculating ZF-based digital precoders within each iteration imposes heavy computational complexity in both approaches.

B. Sorting Algorithm

The sorting algorithm relies on achievable rates of all users, assuming that the users do not cause any interference with each other. This allows us to obtain a diagonal effective channel matrix with $u_{k,ij} = 0$, $\forall i \neq j$, for the k-th PRB and design the digital precoder. Then, we can derive rates, sort them in descending order, and pick M(t) users with the highest rates.

VI. LEARNING-BASED MULTIUSER SCHEDULING

A. Neural Network Setup

To design learning-based scheduling, we employ supervised learning to train a fully connected *deep neural network* (DNN) with L_0 *input features* and I outputs. The DNN consists of *three* hidden layers, where the first, second, and third layers have L_1 , L_2 , and L_3 nodes, respectively. A *sigmoid* activation function is utilized among all layers.

1) Input features: The reasonable set of the input features must encapsulate a combination of the designed analog precoder, i.e., $\mathbf{G}^*(t)$, in Step I of the protocol, the derived effective channel matrix, i.e., $\mathbf{U}_k(I;t)$, in Step II, and the known weights of the users, i.e., $\{w_i(t)\}_{i=1}^I$, from Step IV. Our model takes an input set of features in the form of a vector of size $2I^2 + I(N_{\mathrm{TX}} + 1)$, which is comprised of *four* subvectors. The first and the second subvectors contain the amplitudes and angles of the effective channel averaged over all PRBs, i.e., $\sum_{k=1}^{K} u_{k,ij}/K$, for i, j = 1, 2, ..., I, respectively, each with the size of I^2 . The third subvector encompasses the angles of the analog beams assigned to the users' weights with the size of I. All subvectors are *normalized* to tackle different orders of magnitude between different subvectors.

2) Output decisions: Multiuser scheduling can be seen as a binary classification problem where the users are classified as selected or deselected. We consider that the *i*-th rounded output of the DNN is associated with the selection or deselection of the *i*-th user, where i = 1, 2, ..., I. Let us define α_i as a selection variable for the *i*-th user, where $\alpha_i = 1$ if that user is selected; otherwise, $\alpha_i = 0$. Thus, the set of the scheduled users according to the outputs of the DNN is derived by

$$\mathcal{M}(t) = \{ i \mid \alpha_i = 1, \forall i = 1, 2, ..., I \}.$$
(18)

As the DNN could potentially make an incorrect decision that results in $|\widehat{\mathcal{M}}(t)| > I_{\max}$, we cascade a selection filter with the DNN. The filter sorts the users in $\widehat{\mathcal{M}}(t)$ based on their weights and selects the top I_{\max} of them, which constructs the corresponding $\mathcal{M}(t)$. If $|\widehat{\mathcal{M}}(t)| \leq I_{\max}$, inputs are directly forwarded to the output such that $\mathcal{M}(t) = \widehat{\mathcal{M}}(t)$.

B. Training and Evaluation

A sample set is generated using greedy incremental user scheduling over N_1 episodes, each spanning N_2 slots. Every episode involves varying initial channel realizations, user distributions, and movement directions. It is considered to allocate a fraction $0 \le \beta \le 1$ of the generated samples for training the model while reserving the remaining $1 - \beta$ for evaluating the trained model. We break the training set into batches of size N_3 and train the model for N_4 epochs. We use the *cross-entropy loss* function to evaluate performance.

VII. NUMERICAL RESULTS

A. Setup and Assumptions

We assume I = 20 users, each with a single antenna, i.e., $N_{\rm RX} = 1$, are randomly distributed around the BS in a circular area of 100 [m] radius. The BS is assumed to be located at a height of 7 [m]. Its antenna array has $N_{\rm TX} = 16$ antennas arranged in a uniform planar array (UPA) structure, with 8 elements in the horizontal and 2 in the vertical. The antenna boresight of the BS is tilted downward by 10° , where the BS can cover horizontally from -180° to 180° and vertically from -30° to 30° . The analog precoding codebook, i.e., \mathcal{G} , consists of a 32×8 grid of beams evenly spaced in the horizontal and vertical directions. Regarding the OFDM technology, we adopt numerology $\mu = 5$ from 5G NR [17], where a subframe consists of 32 slots. Every slot contains 14 OFDM symbols, each having a duration of 2.23 [μ sec] including a CP of 0.15 [μ sec]. Also, 12 subcarriers build one PRB. This results in a subcarrier spacing (SCS) of 480 [KHz] and bandwidth factor $B_k = 168$ for k =1, 2, ..., K. Unless otherwise specified, we use the remaining parameter values listed in Table I.

B. Channel Model

We use the mmWave channel model from [12, Eq. (9)] to derive the channel matrix, i.e., $\mathbf{h}_{k,i}(t)$, between the BS and the *i*-th user within the *k*-th PRB at the *t*-th. Accordingly, we consider the same large-scale parameters as given in [12] for a carrier frequency of $f_c = 28$ [GHz]. However, to model the small-scale fading, we assume 20 subpaths within each cluster

TABLE I: Parameters for Numerical Results

Name	Symbol	Value
No. RF chains at the BS	N _{RF}	8
Maximum no. served users	I _{max}	8
Power limit at the k-th PRB	P_k	20 [dBm]
Noise power at the i_m user	$\sigma_{i_m}^2$	-30 [dBm]
Carrier frequency	f_c	28 [GHz]
No. PRBs	K	12
No. OFDM subframes per frame	—	10
Duration of each OFDM subframe	_	10^{-3} [sec]
No. long-time blocks	-	100
No. slots per long-time block	$N_{\rm SB}$	1
No. input features in the DNN	L_0	1140
No. nodes in the DNN's hidden layers	(L_1, L_2, L_3)	(1200, 500, 200)
No. sampling episodes	N_1	120
No. slots per sampling episode	N_2	100
Sample splitting fraction	β	0.8
Length of each DNN training batch	N_3	16
No. DNN training epochs	N_4	300

and a maximum *Doppler shift* of $f_{c,\max} = 258$ [Hz] concerning the carrier frequency. Since the Doppler shift is a function of frequency, its value changes among different PRBs, each having a bandwidth of 12×480 [KHz]. In this sense, for modeling $\mathbf{h}_{k,i}(t)$, the induced Doppler shift $f'_{k,\max}$ [Hz] based on the central frequency of the k-th PRB is given as follows

$$f_{k,\max}' = f_{c,\max}\left(1 + \frac{\Delta f_k}{f_c}\right) = 258\left(1 + \frac{\Delta f_k}{28\,[\text{GHz}]}\right) \quad (19)$$

where Δf_k is equal to the subtraction of the k-th PRB's central frequency from the carrier frequency.

C. Results and Discussion

In Fig. 3 (a), we analyze the impact of increasing the maximum number of users that can be served per slot, i.e., I_{max} , on the offered PF using different user scheduling approaches. The graph indicates that the incremental algorithm yields the highest PF, followed by the decremental algorithm. The learning-based approach shows moderate performance compared to the others, particularly for higher I_{max} . Both greedy algorithms are flexible to refrain from selecting more users if adding them worsens the interference, leading to a reduced achievable rate and PF. The learning-based approach also possesses this adaptability. On average, the incremental, decremental, and learning-based approaches select 18.8%, 29.49%, and 16.62% of the users, respectively. In contrast, the sorting and random approaches blindly schedule all possible users to be served.

The run time of each user scheduling algorithm considering the maximum number of users that can be served is depicted in Fig. 3 (b). The decremental approach comes with a significant disadvantage in terms of long run time, resulting in much higher complexity than the others. The learning-based and random scheduling approaches require the shortest run time, independent of I_{max} . The sorting algorithm takes longer, and the incremental one lies in between, with its run time increasing as I_{max} increases from 1 to 5. After that, the run time remains constant, as the algorithm chooses not to select more users to



Fig. 3: The impact of the maximum number of users served per slot on (a) the average PF and (b) the required run time of the algorithms, alongside (c) the trade-off between their average performance and run time.



Fig. 4: Timing profiles of the main user scheduling components.

keep the induced interference low. The same reasoning applies to the decremental approach for $I_{\text{max}} > 10$.

In Fig. 3 (c), the *trade-off* between performance, measured as the average PF or sum-rate, and complexity, in terms of the average run time, for different user scheduling approaches is demonstrated. The most suitable approach is selected based on the key criterion of interest. For example, the incremental (decremental) approach provides 1.76 (1.47) times higher PF at the cost of 2.3 (16.1) times longer run time compared to the learning-based one. Therefore, greedy scheduling is selected *if* a higher PF is more important; otherwise, learning-based scheduling might offer a much shorter run time.

Moreover, Fig. 4 displays the timing profiles of the three main components involved in scheduling users within a short-length block. We observe that the longer time the incremental and decremental algorithms take to run is not only due to user search but also because of the time needed to obtain effective channel matrices and calculate the precoding matrix in each iteration. This confirms the higher complexity of the greedy incremental and decremental algorithms (see Section V-A).

VIII. CONCLUSION

We studied the multiuser scheduling challenge in mmWave MIMO-OFDM systems with hybrid beamforming. We defined PF as a long-term evaluation metric and formulated the optimization problem aimed at maximizing PF by optimally designing the digital and analog precoders, as well as scheduling the users to be served by the BS. To achieve this, we tailored a two-timescale protocol and implemented various scheduling methods, including greedy and learning-based approaches. Our results demonstrated the trade-off between performance and computational complexity for each approach. Additionally, we observed that the learning-based approach strikes a favorable balance between the average PF and the required run time.

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